

SUPPLEMENTAL MATERIALS

Movie S1. Flagellar beat pattern of a wild-type cell. Playback speed is 15fps.

Movie S2. Flagellar beat pattern of a *bop5-3* mutant. Playback speed is 30fps.

Movie S3. Flagellar beat pattern of *pf9-3* mutant. Playback speed is 30fps

Movie S4. Phototaxis of wild-type and *bop5-3*.

Table S1. Statistical analysis of forward swimming velocities.

	<i>wild-type</i>	<i>pf9-3</i>	<i>bop5-1</i>	<i>bop5-3</i>	<i>bop5-4</i>	<i>bop5-6</i>	<i>bop5-3</i> <i>::IC138</i> <i>2D1</i>	<i>bop5-3</i> <i>::IC138</i> <i>2E1</i>
<i>wt</i>	NA	<0.005	<0.005	<0.005	<0.005	<0.005	<0.005	<0.005
<i>pf9-3</i>		NA	<0.005	<0.005	<0.005	<0.005	<0.005	<0.005
<i>bop5-1</i>			NA	<0.005	<0.005	<0.005	<0.005	<0.005
<i>bop5-3</i>				NA	<0.005	<0.005	<0.005	<0.005
<i>bop5-4</i>					NA	<0.005	<0.005	<0.005
<i>bop5-6</i>						NA	<0.005	<0.005
<i>Bop5-3</i> <i>::IC138 2D1</i>							NA	0.832

The swimming velocities of all strains shown in Figure 4A were compared using F-tests and T-tests, and the P values are shown here. The samples were scored as significantly different at P values less than 0.005. Because of the large sample sizes (N=190 to 552), small but significant differences were noted between all strains with respect to swimming velocities. The IC138 rescued strains are significantly faster than the *bop5-3* mutant (and other *bop5* mutants), not significantly different from one another, and slightly but significantly slower than wild-type.

Table S2. Statistical analysis of *in vitro* microtubule sliding velocities

	<i>wild-type</i>	<i>ida2-6</i>	<i>bop5-1</i>	<i>bop5-3</i>	<i>bop5-4</i>	<i>bop5-6</i>	<i>bop5-3</i> <i>::IC138</i> <i>2D1</i>	<i>bop5-3</i> <i>::IC138</i> <i>2E1</i>
<i>wt</i>	NA	<0.005	<0.005	<0.005	<0.005	<0.005	0.007	0.036
<i>ida2-6</i>		NA	0.263	0.581	0.142	0.600	<0.005	<0.005
<i>bop5-1</i>			NA	0.513	<0.005	0.515	<0.005	<0.005
<i>bop5-3</i>				NA	0.013	0.991	<0.005	<0.005
<i>bop5-4</i>					NA	0.012	<0.005	<0.005
<i>bop5-6</i>						NA	<0.005	<0.005

The *in vitro* microtubule sliding velocities of all strains shown in Figure 4C were compared using T-tests and the P values are shown here. Samples were scored as significantly different at P values less than 0.005. All of the mutants are significantly slower than wild-type. The differences in sliding velocities between the mutant strains are not statistically significant, except for the difference between *bop5-4* and *bop5-1*. The sliding velocities of the IC138 rescued strains are significantly faster than *bop5-3*.

Table S3. Additional waveform parameters.

	Significantly influenced by flagellar length?	Wild-type	<i>bop5-3</i>	<i>ida3</i>
Avg. propagation speed of R bend ($\mu\text{m/s}$)*	Yes	1449.7 +/- 240.2	1074.8 +/- 198.5	1140.2 +/- 111.0
Avg. propagation speed of P bend ($\mu\text{m/s}$)	Yes	1411.7 +/- 191.8	1240.4 +/- 268.8	1506.0 +/- 191.6
Avg. min. (R) curvature-physical ($\text{rad}/\mu\text{m}$)+	Yes	-0.55 +/- 0.08	-0.60 +/- 0.04	-0.50 +/- 0.06
Avg. max. (P) curvature-physical ($\text{rad}/\mu\text{m}$)+	No	0.20 +/- 0.04	0.18 +/- 0.03	0.22 +/- 0.03
Initial delay between P and R bends (cyc)+	N/A	0.44 +/- 0.02	0.40 +/- 0.07	0.32 +/- 0.04

Parameters where values for *bop5-3* and *ida3* were significantly different from wild-type are marked with an asterisk. Parameters where values for *bop5-3* and *ida3* were significantly different from each other are marked with a plus sign ($p < 0.05$).